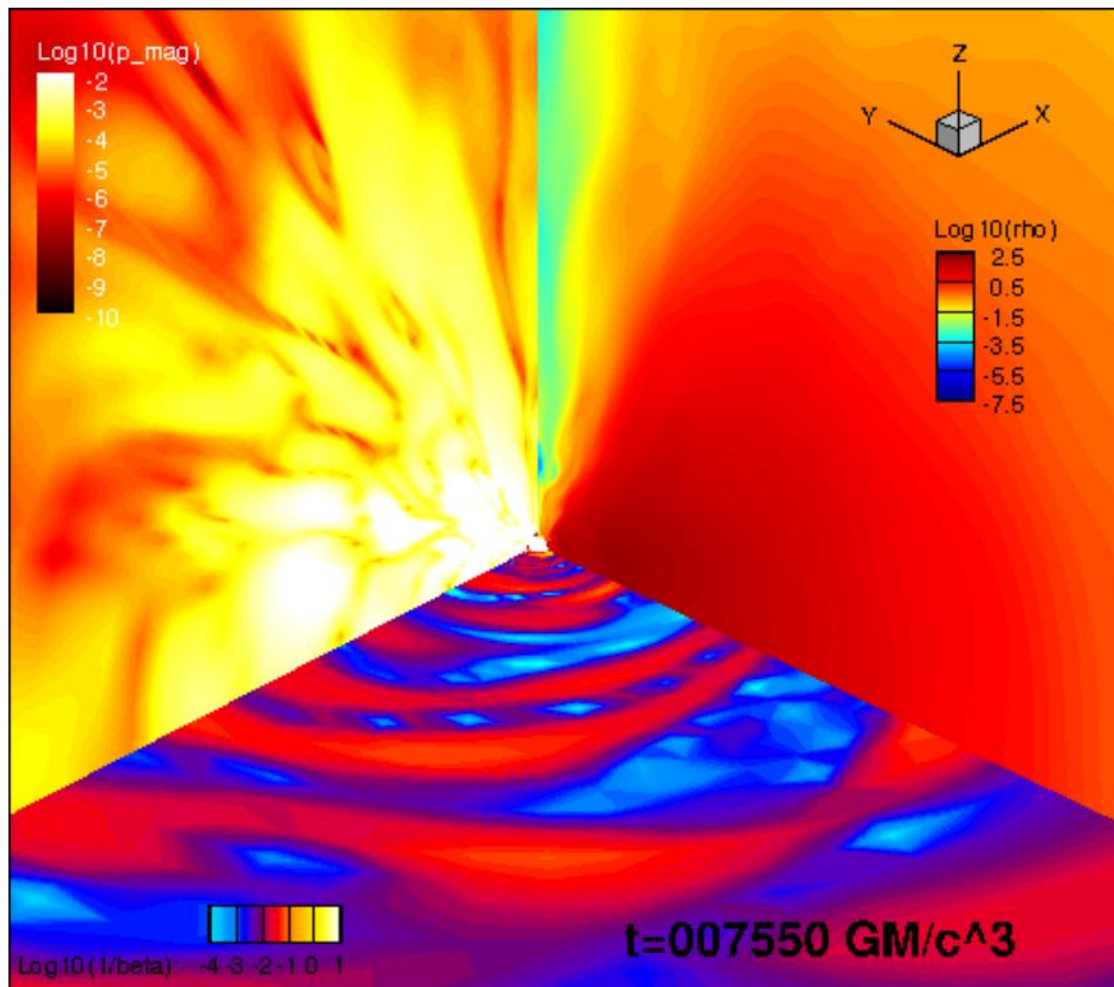


大質量ブラックホール降着円盤から放出される大強度アルフヴェンパルスとジェット



水田 晃(理化学研究所)

References

AM, Ebisuzaki Tajima Nagataki,
MNRAS 479 2534(2018)

the case of spin $a=0.9$

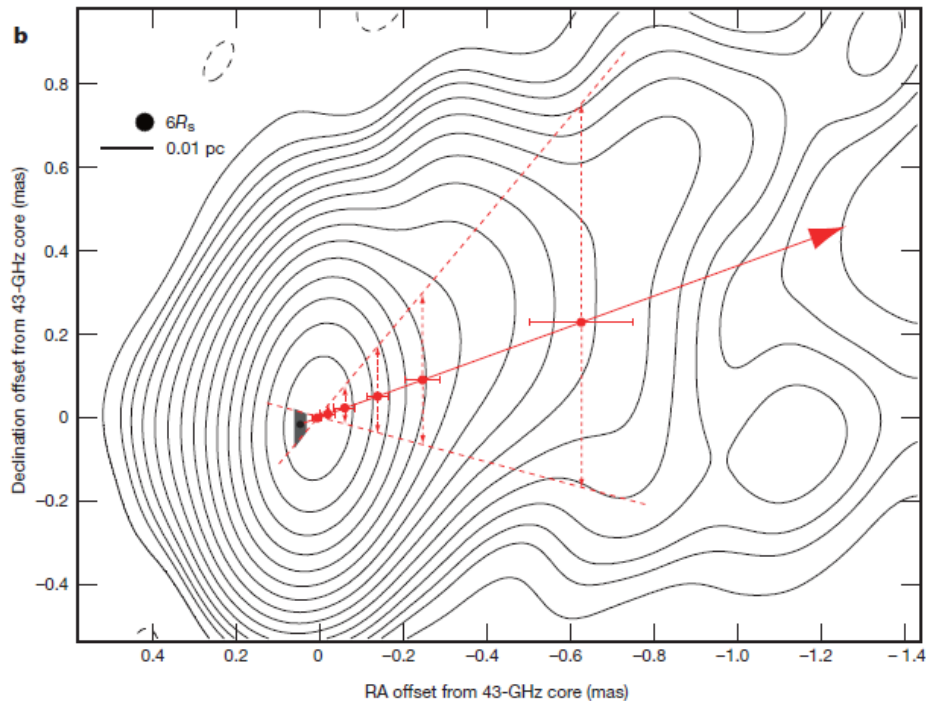
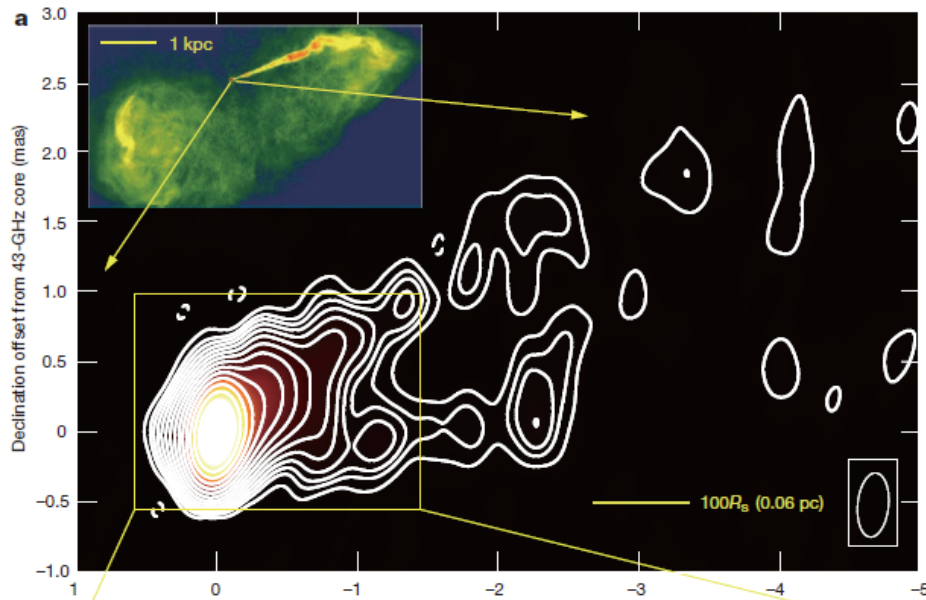
AM+ in prep.

parameter study in spin a

CFCAユーザーズミーティング
@国立天文台(三鷹)

2019.01.15

Active Galactic Nuclei Jet



Hilghlly collimated outflows from center of galaxy

- central engine
supermassive black hole

+

accretion disk

- relativistic outflows

Bulk Lorentz factor : $\Gamma \sim 10$

- multiwavelength emission
radio to high energy γ -rays

- strong candidate of
ultra high energy cosmic ray
accelerator

via Fermi acc. ? (1954)

wake field acc.

(Ebisuzaki & Tajima 2014)

M87 radio observation Hada +(2011)

ブラックホール降着円盤とジェット形成

中心エンジン (Black Hole(BH) + disk)

- 円盤の時間変動 (Shibata +1990,
Balbus & Hawley1991)

-- MRI growth ($B \nearrow \Rightarrow$ Low beta state)

Magnetorotational instability (磁気回転不安定性)

- 差動回転: $d\Omega_{\text{disk}}/dr < 0$

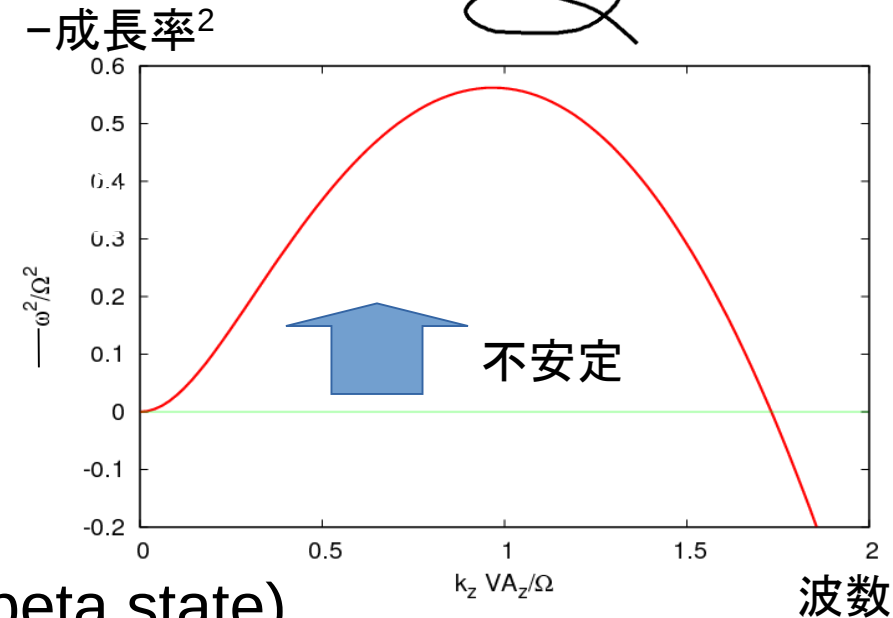
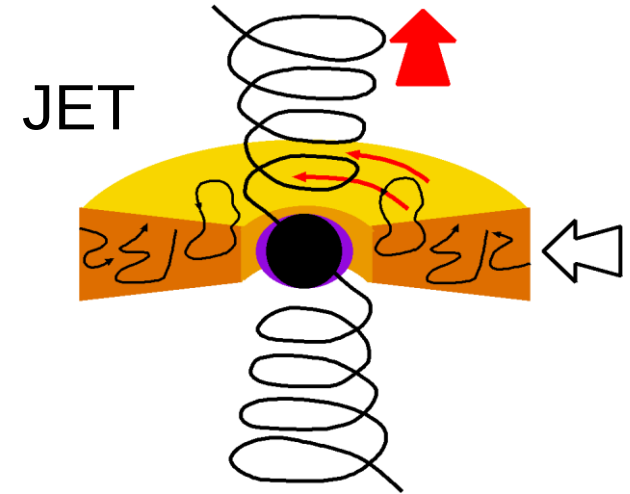
$\Omega_{\text{disk}} \propto r^{-1.5}$: Kepler rotation

- $B \propto \exp(i\omega t)$ 指数関数的増幅

Unstable @ $0 < kV_a < 1.73 \Omega_K$

Most unstable @ $kV_a \sim \Omega_K$ $\omega \sim 0.75\Omega_K$

- MRI によって角運動量輸送



-- 磁気エネルギーの散逸 ($B \searrow \Rightarrow$ High beta state)

-- 円盤鉛直方向に Strong Alfvén burst (Low $\beta \Rightarrow$ High β)
ジェット中を伝播し、wake field 加速機構による宇宙線の起源や
ブレーザー天体の短時間変動 (Ebisuzaki +2014, A.M2018)

Basic Equations : GRMHD Eqs.

GM=c=1, a: dimensionless Kerr spin parameter

$$\frac{1}{\sqrt{-g}} \partial_\mu (\sqrt{-g} \rho u^\mu) = 0$$

Mass conservation Eq.

$$\partial_\mu (\sqrt{-g} T^\mu_\nu) = \sqrt{-g} T^\kappa_\lambda \Gamma^\lambda_{\nu\kappa}$$

Energy-momentum conservation Eq.

$$\partial_t (\sqrt{-g} B^i) + \partial_j (\sqrt{-g} (b^i u^j - b^j u^i)) = 0$$

Induction Eq.

$$p = (\gamma - 1) \rho \epsilon \quad \text{EOS } (\gamma=4/3)$$

Constraint equations.

$$\frac{1}{\sqrt{-g}} \partial_i (\sqrt{-g} B^i) = 0 \quad \text{No-monopoles constraint}$$

$$u_\mu b^\mu = 0 \quad \text{Ideal MHD condition}$$

$$u_\mu u^\mu = -1 \quad \text{Normalization of 4-velocity}$$

Energy-momentum tensor

$$T^{\mu\nu} = (\rho h + b^2) u^\mu u^\nu + (p_g + p_{\text{mag}}) g^{\mu\nu} - b^\mu b^\nu$$

$$p_{\text{mag}} = b^\mu b_\mu / 2 = b^2 / 2$$

$$b^\mu \equiv \epsilon^{\mu\nu\kappa\lambda} u_\nu F_{\lambda\kappa} / 2 \quad B^i = F^{*it}$$

GRMHD code (Nagataki 2009,2011)

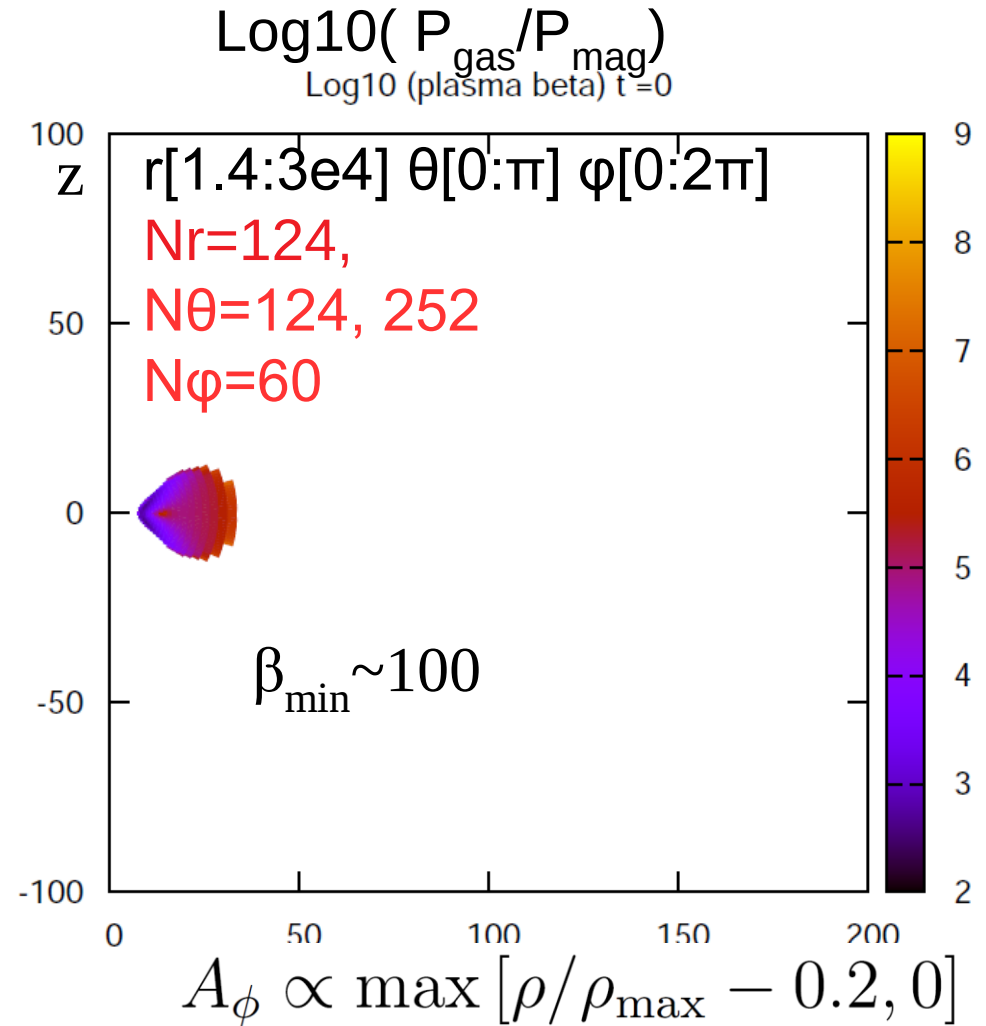
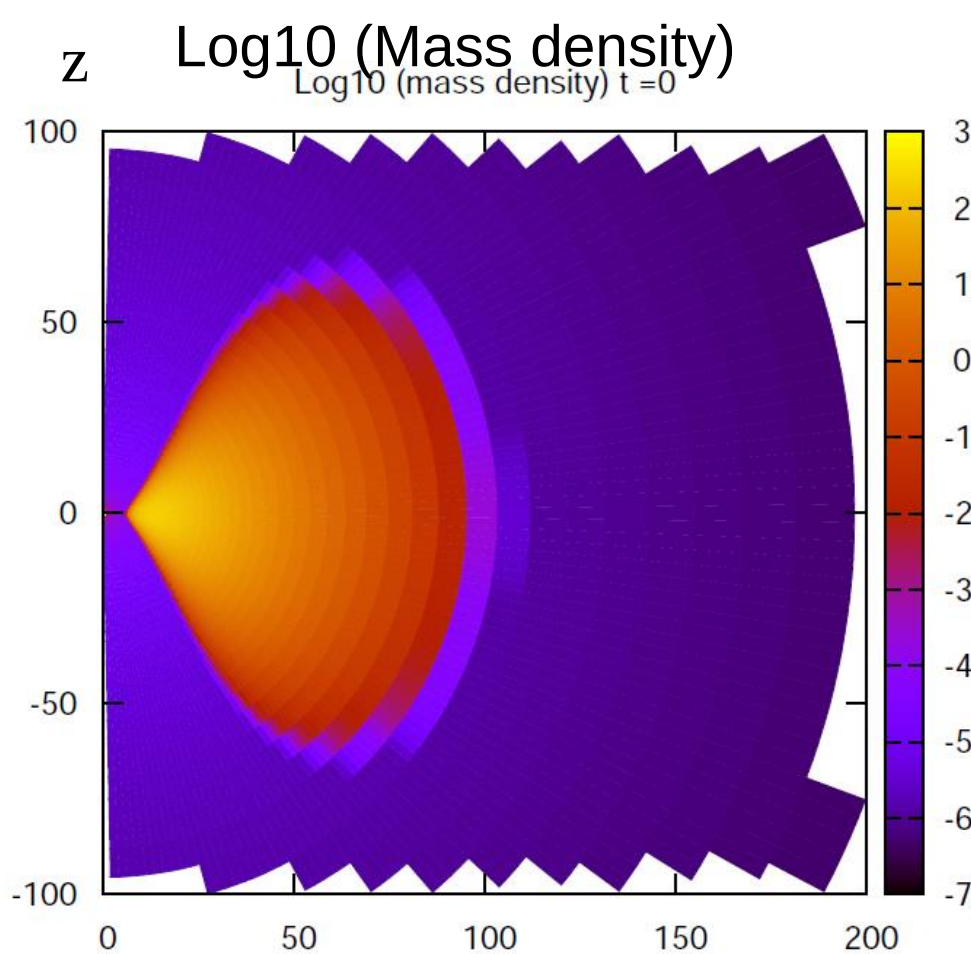
Kerr-Schild metric (no singular at event horizon)

HLL flux, **2nd** order in space (van Leer), **2nd** or 3rd order in time

See also, Gammie +03, Noble + 2006

Flux-interpolated CT method for divergence free

Initial Condition



Fisbone-Moncrief (1976) solution – hydrostatic solution of tori around rotating BH ($a=0.9$, $r_H \sim 1.44$), $l_* \equiv -u^t u_\phi = \text{const} = 4.45$, $r_{\text{in}} = 6. > r_{\text{ISCO}}$
With maximum 5% random perturbation in thermal pressure.

Units $L : R_g = GM/c^2 (=R_s/2)$, $T : R_g/c = GM/c^3$, mass : scale free
 $\sim 1.5 \times 10^{13} \text{cm} (M_{\text{BH}}/10^8 M_{\text{sun}})$ $\sim 500 \text{s} (M_{\text{BH}}/10^8 M_{\text{sun}})$

Grids to capture MRI fastest growing mode

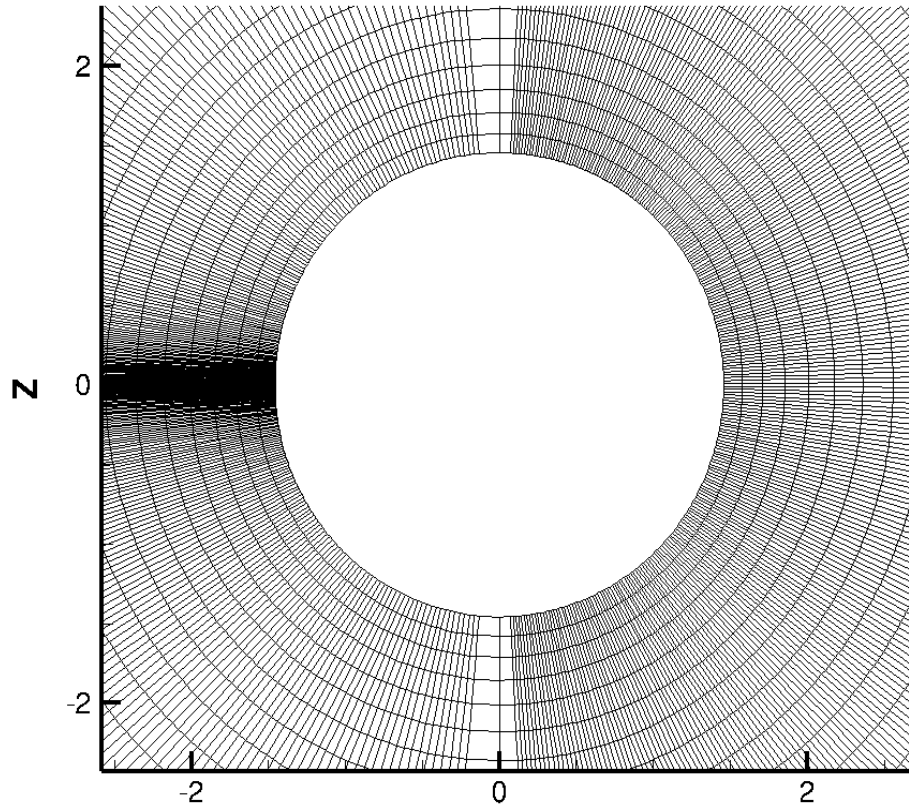
Wavelength of fastest growing mode in the disk

$$\lambda_{\text{MRI}} = 2\pi \langle C_{\text{az}} \rangle / \Omega_K(R) \sim 0.022 (R/R_{\text{ISCO}})^{1.5}$$

$$\langle C_s \rangle \sim \langle C_{\text{Az}} \rangle \sim 10^{-3} c$$

$$R_{\text{ISCO}} (a=0.9) = 2.32$$

$$N_\theta = 252$$



$$\theta = \pi x_2 + \frac{1}{2}(1-h) \sin(2\pi x_2) \quad \Delta\theta = \text{cost}$$

$$x_2 = [0:1] \quad \Delta x_2 = \text{cost} \quad h=1$$

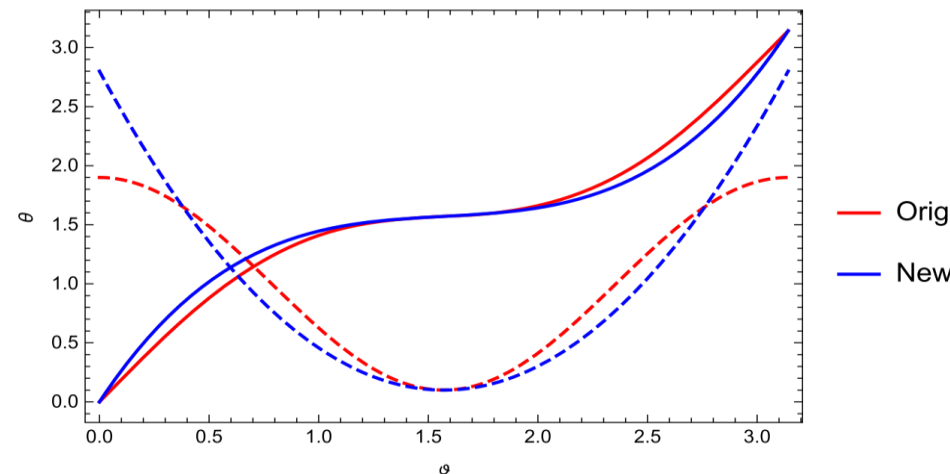
$$h=0.2$$

McKinney and Gammie



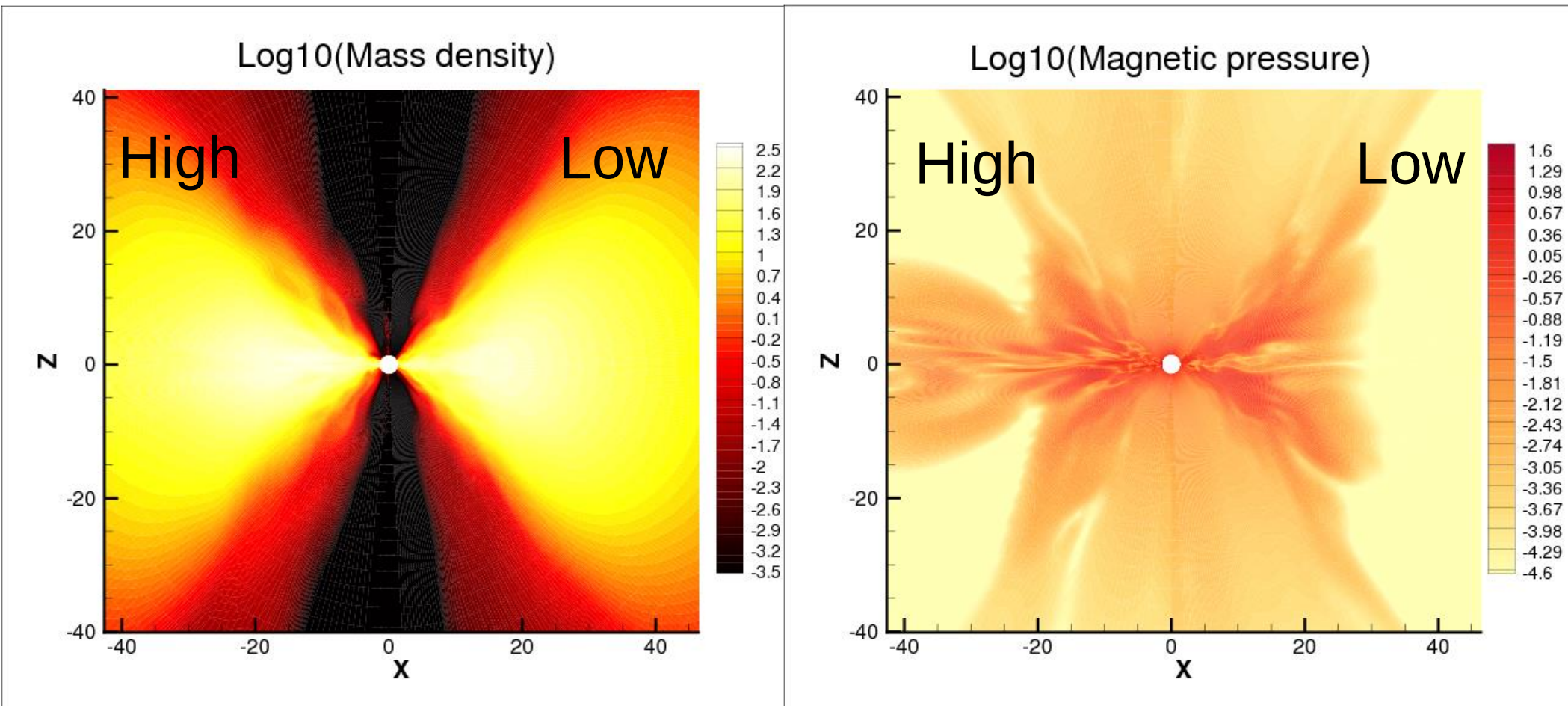
Any coordinates described by analytic function can be applied (generalized curvilinear coordinates)

$$\theta_{\text{KS}}(\vartheta) = \vartheta + \frac{2h\vartheta}{\pi^2} (\pi - 2\vartheta)(\pi - \vartheta).$$

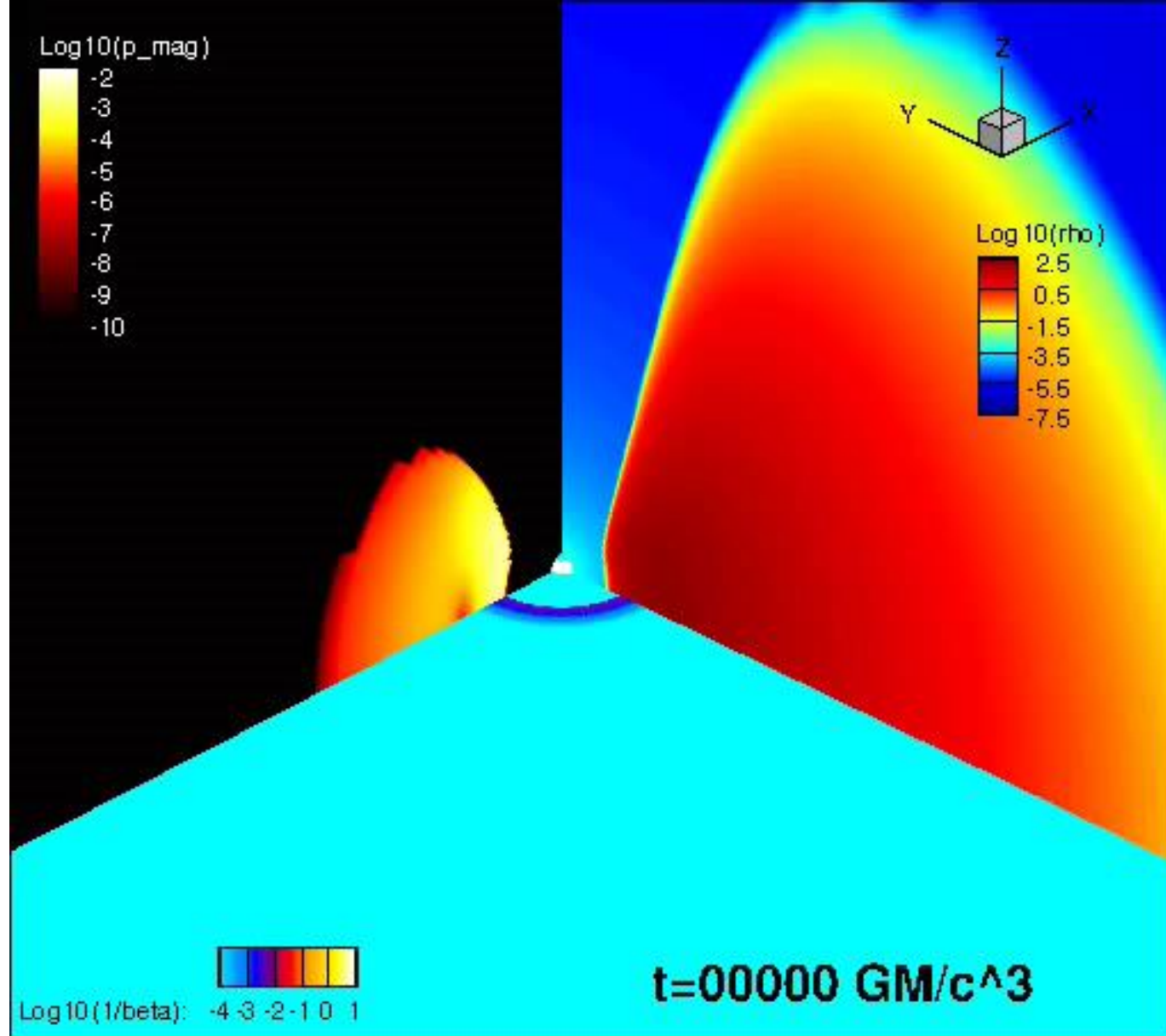


Porth + 2017

Higher resolution calculation in θ around equator

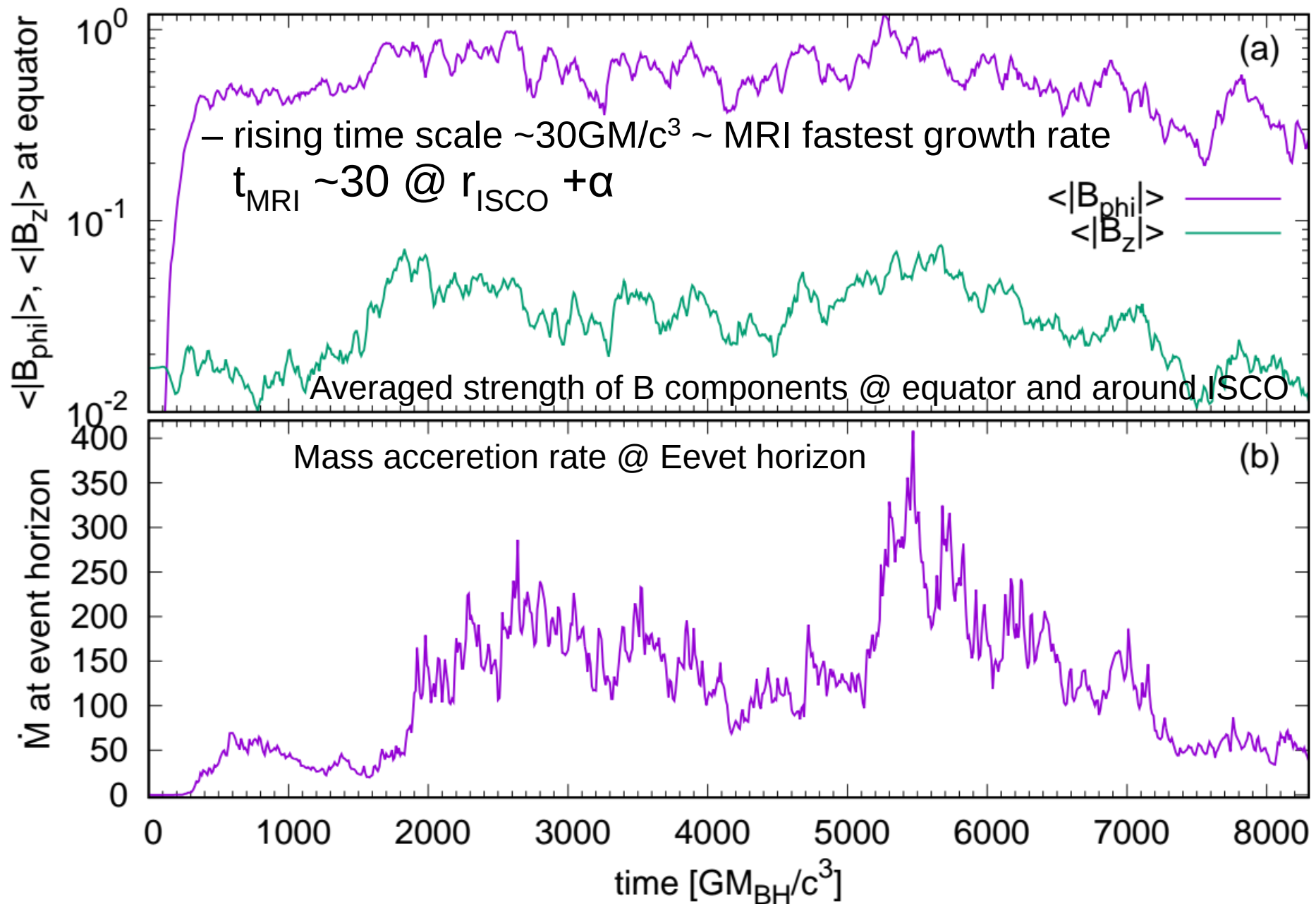


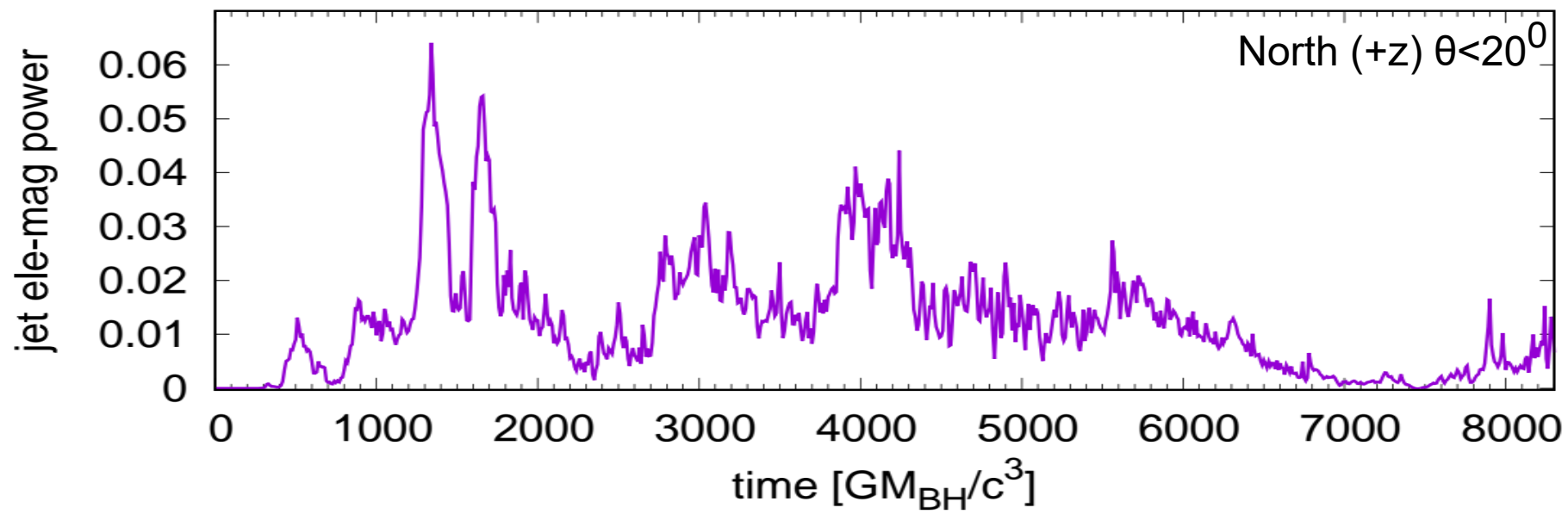
Right : about 8 times higher resolution in θ @ equator

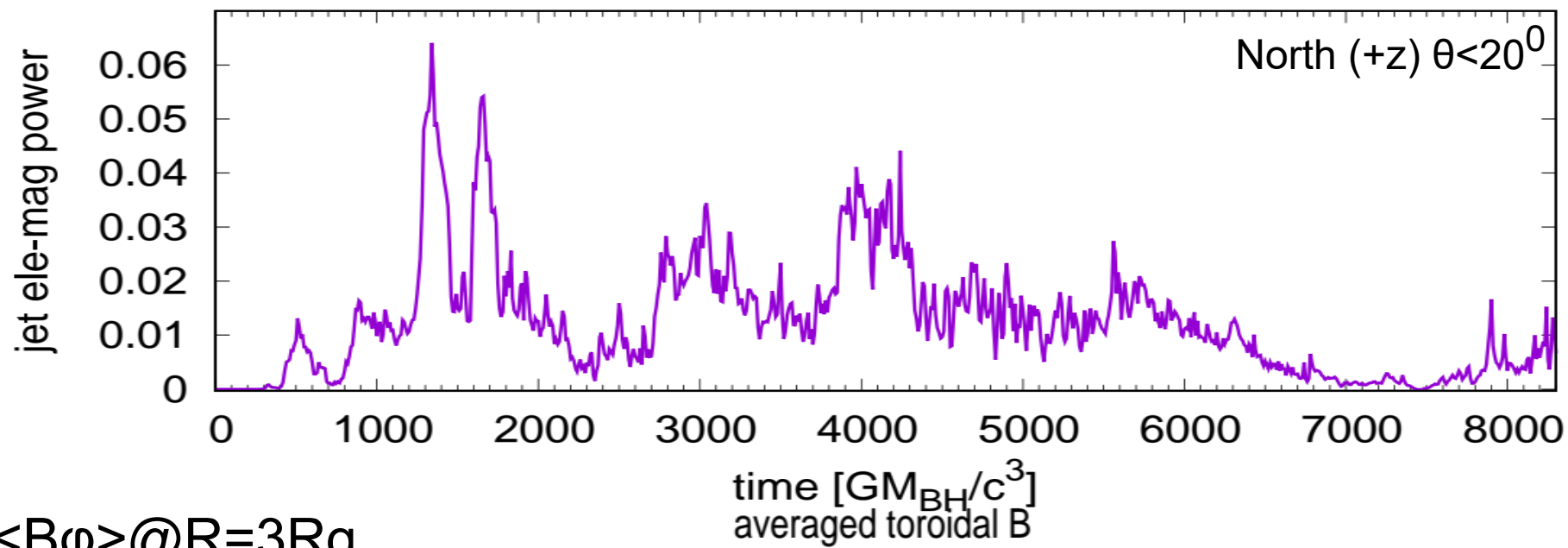


Disk : Fishbone Moncrief solution, spin parameter **$a=0.9$ (0.7, 0.5, 0.3, 0.1)**
spherical coordinate $R[0.98 r_H(a):3e4]$ $\theta[0:\pi]$ $\phi[0:2\pi]$
[$NR=124$, **$N\theta=252$** , **$N\phi=60$**] $r=\exp(n_r)$, θ : **non-niform (concentrate @ equator)**
 $d\phi \sim 6^\circ$: uniform Poloidal B field, $\beta_{\min}=100$

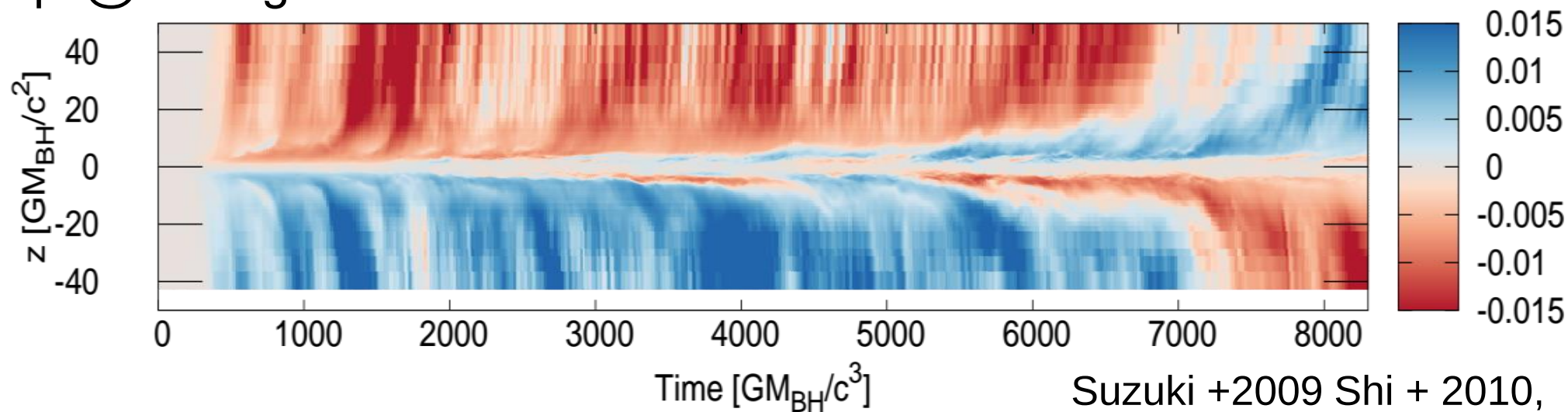
B-field amplification & mass accretion



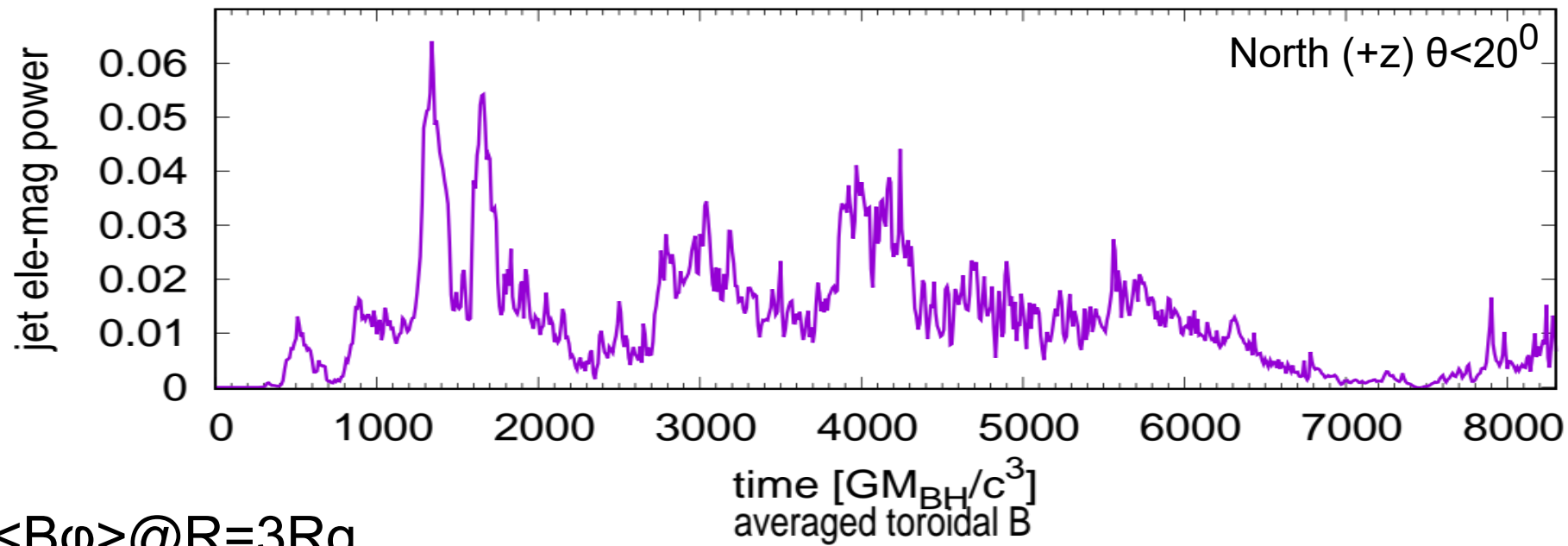




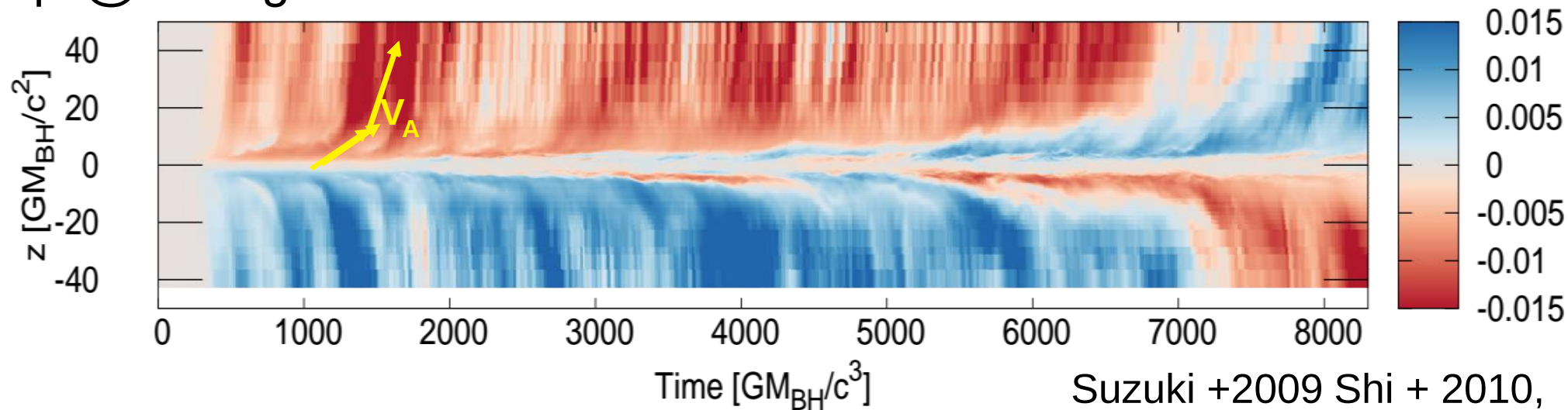
$\langle B_\phi \rangle @ R=3R_g$



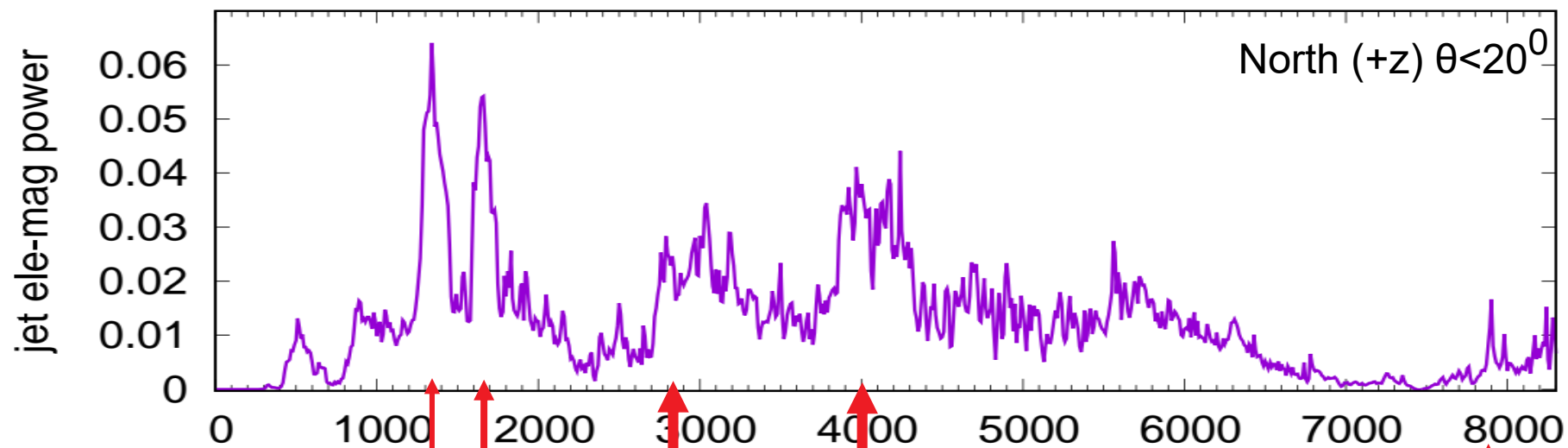
Suzuki +2009 Shi + 2010,
Machida +2013



$\langle B_\phi \rangle @ R=3R_g$

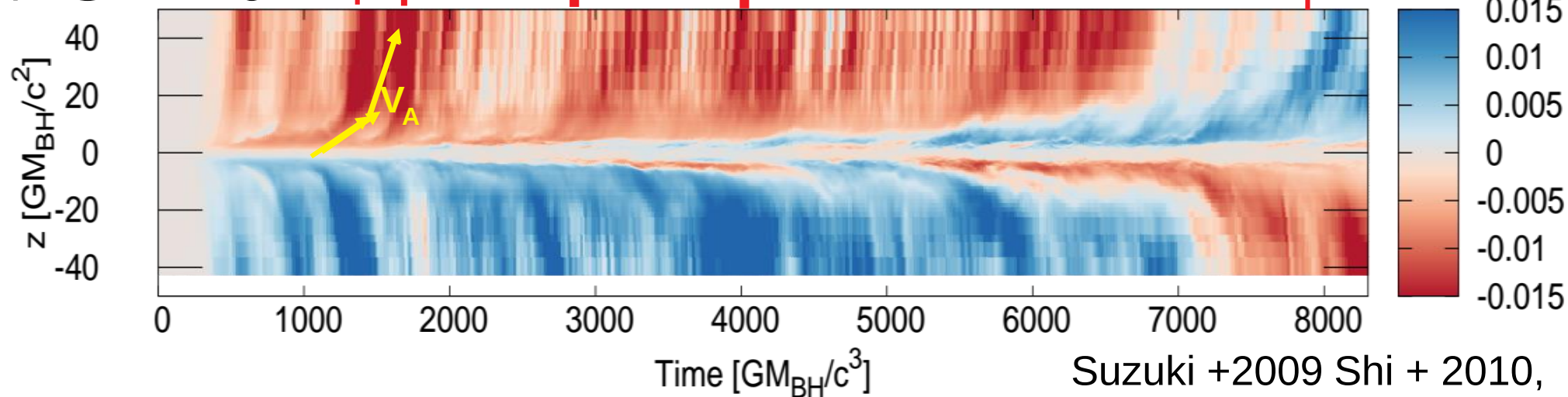


Suzuki +2009 Shi + 2010,
Machida +2013

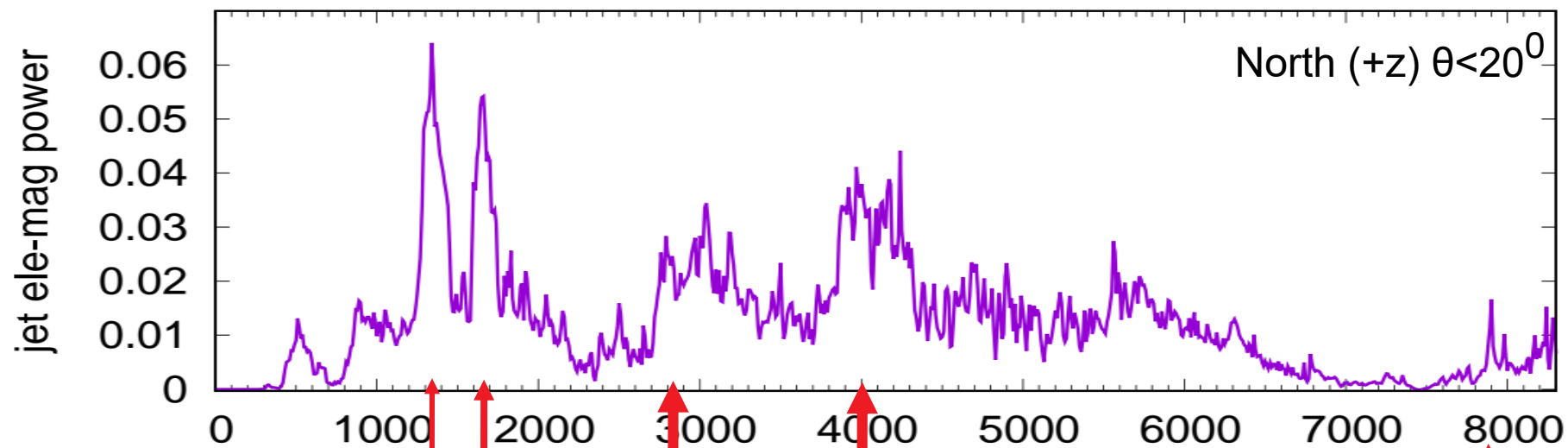


averaged toroidal B

$\langle B_\phi \rangle @ R=3R_g$

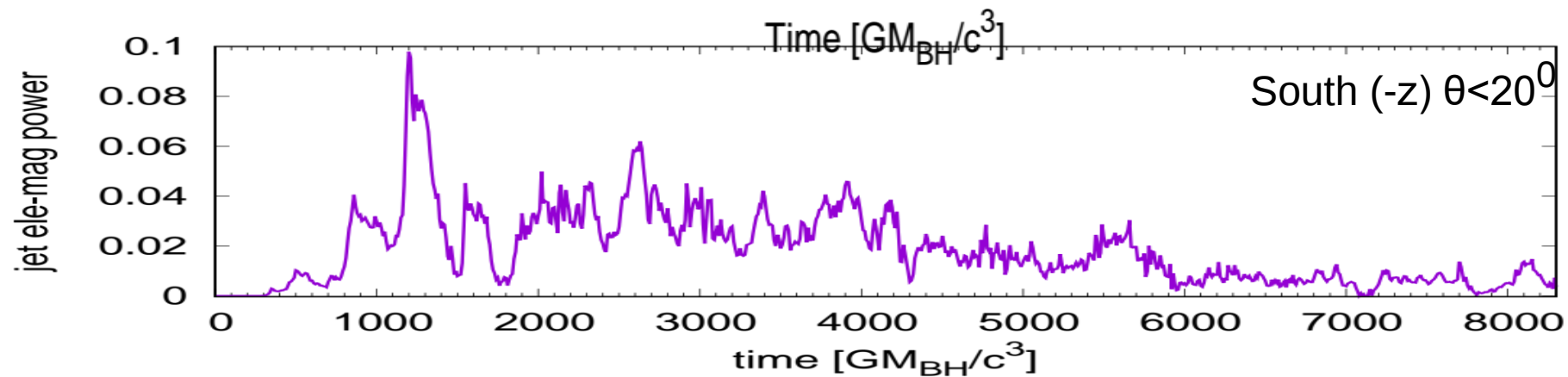
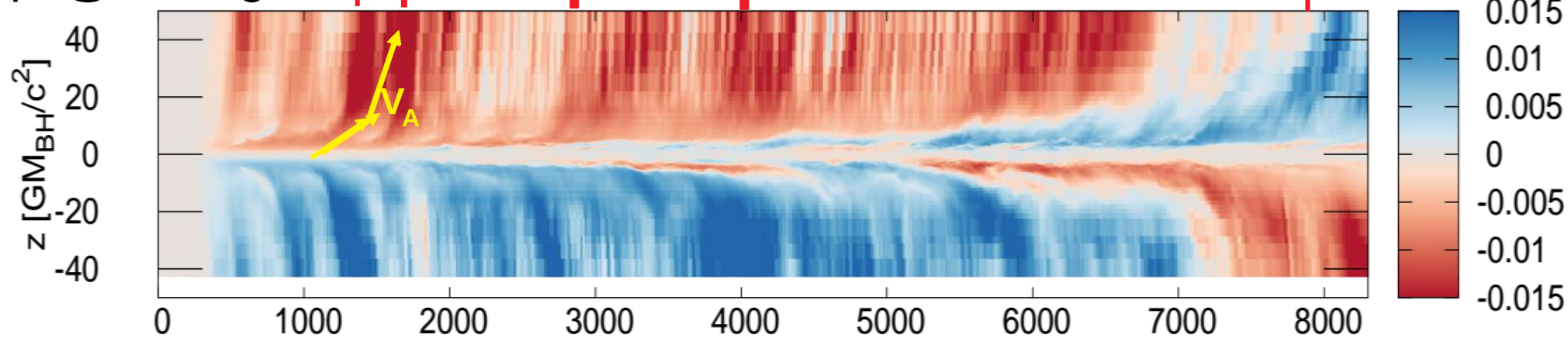


Suzuki +2009 Shi + 2010,
Machida +2013
Takasao+2018 =>後述

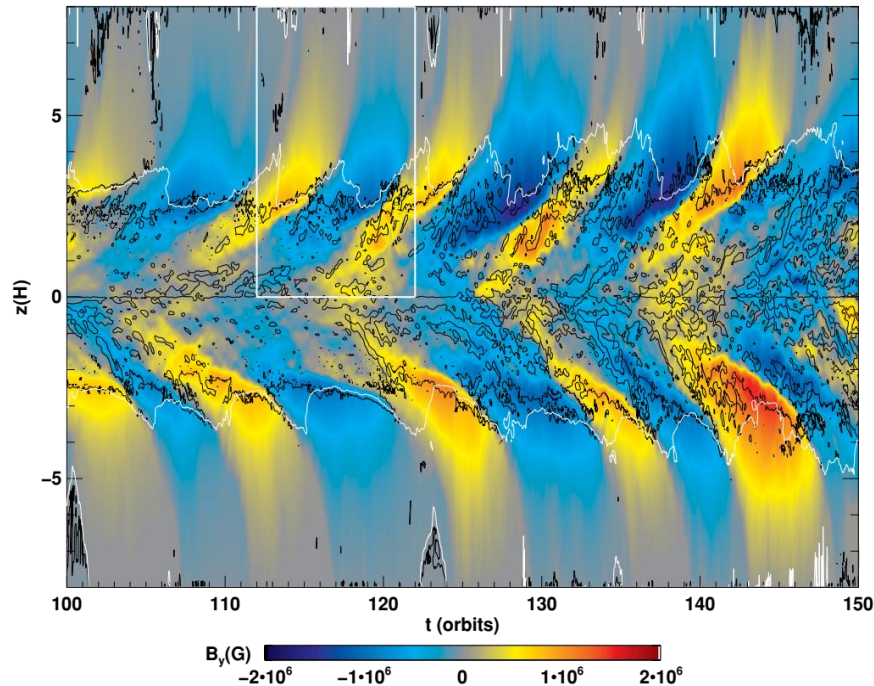


$\langle B_\phi \rangle @ R=3R_g$

averaged toroidal B



Butterfly diagram is common feature of accretion disk

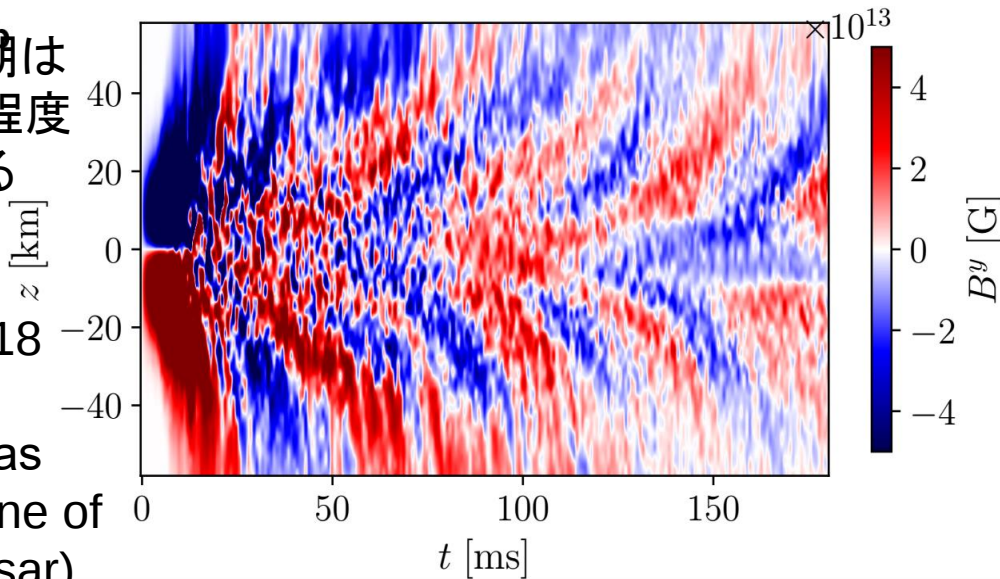


Shi + 2011

Local box sim.

Protostellar disk

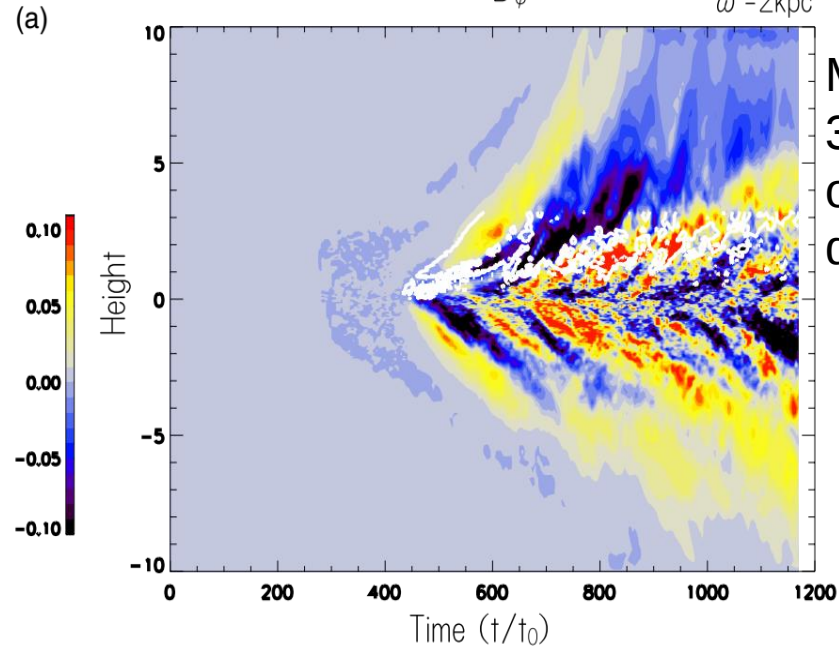
繰り返し周期は
10回転周期程度
極性が変わる



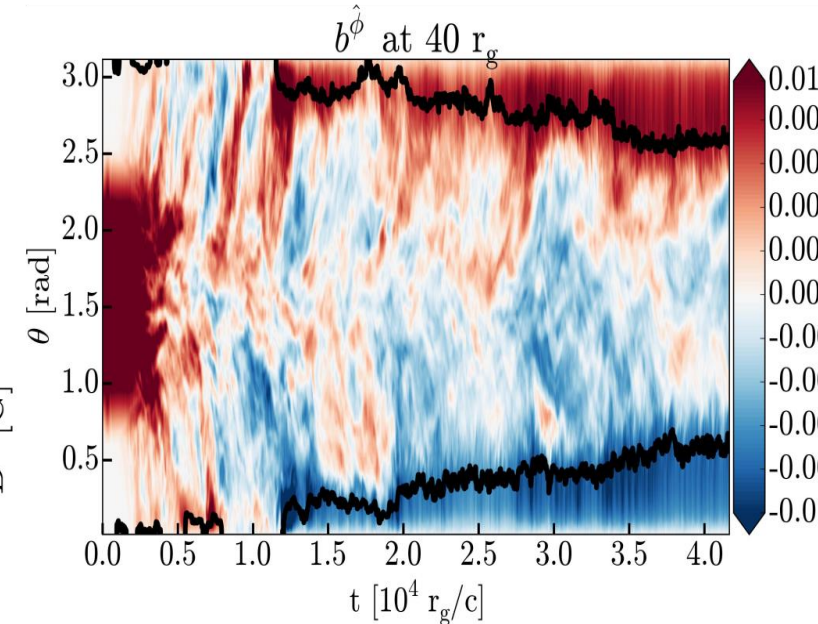
Siegel + 2018

GRMHD

+ v cooling as
central engine of
GRB(collapsar)

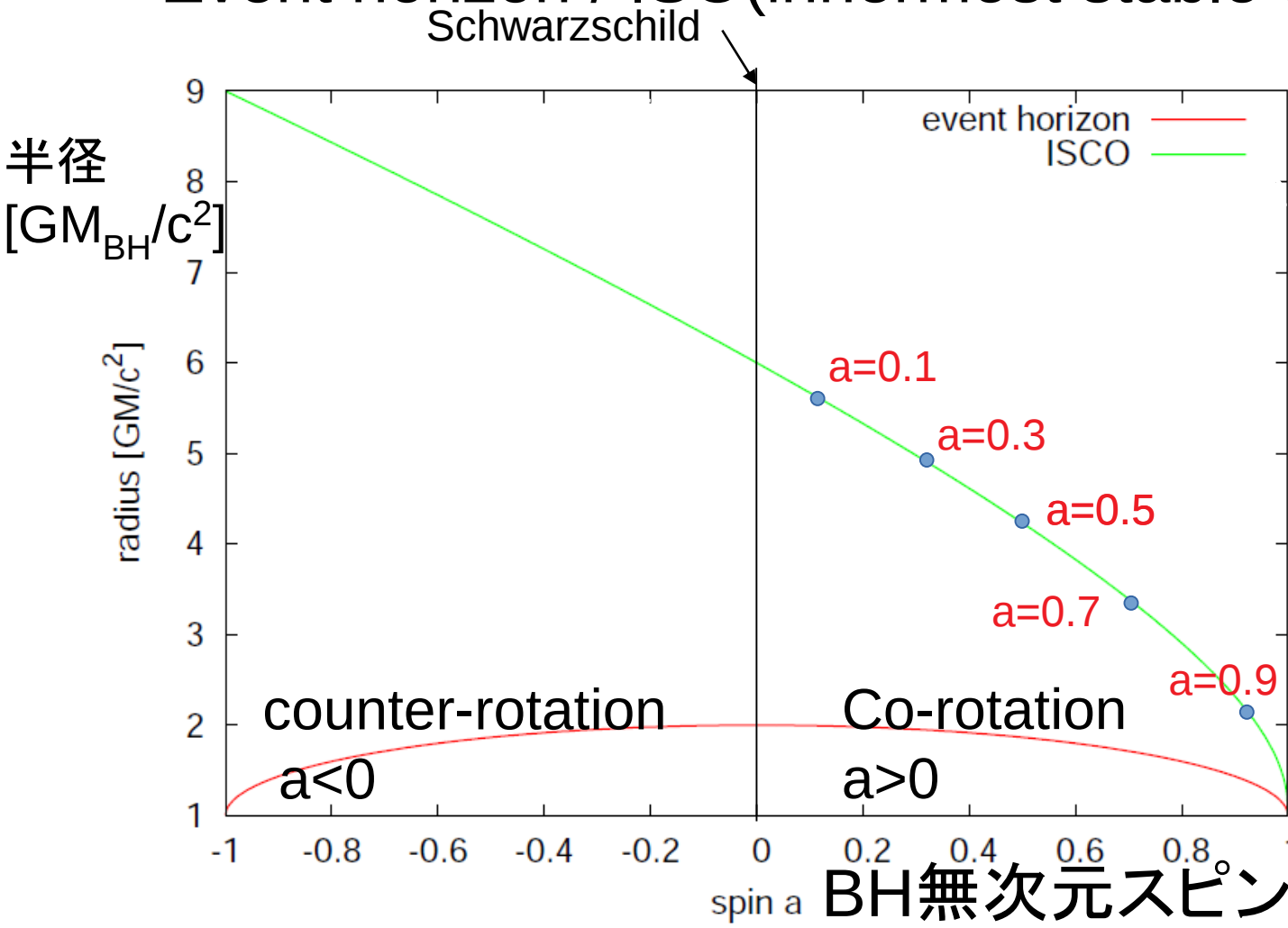


Machida + 2013
3D MHD sim
of galactic
dynamo



Liska + 2018
GRMHD+AMR

Event horizon / ISO(innermost stable circular orbit)



Both r_H and r_{ISCO} approaches $r=1$ as $a \rightarrow 1$ (maximum spin)

• Since B-field amplification occurs in the disk ($r > r_{ISCO}$), the timescale of B-field amplification may depends on Kerr-spin parameter.

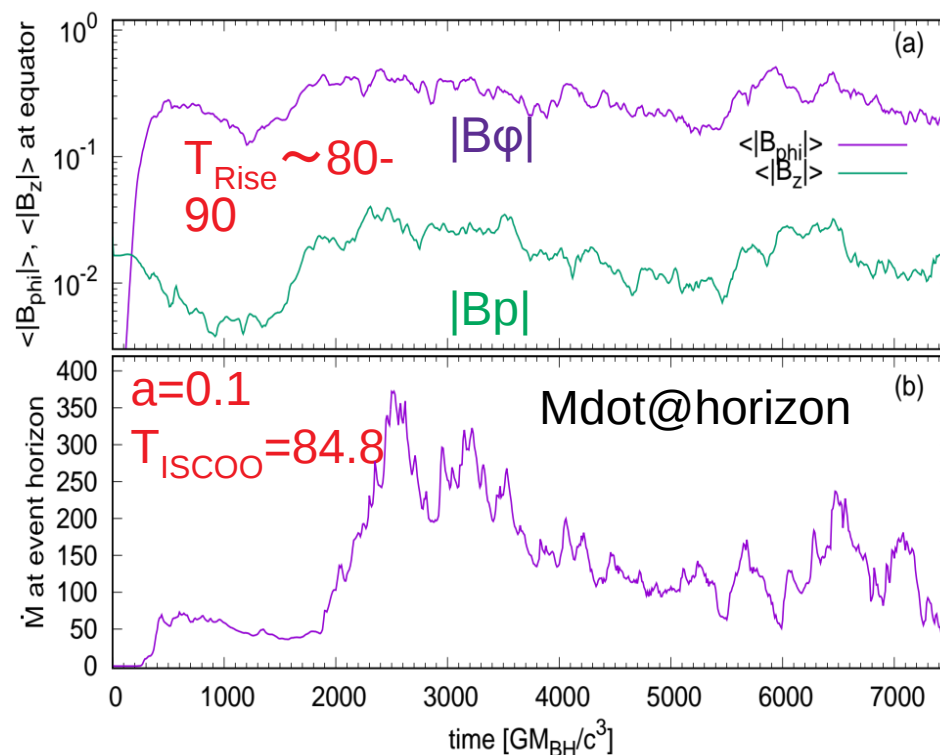
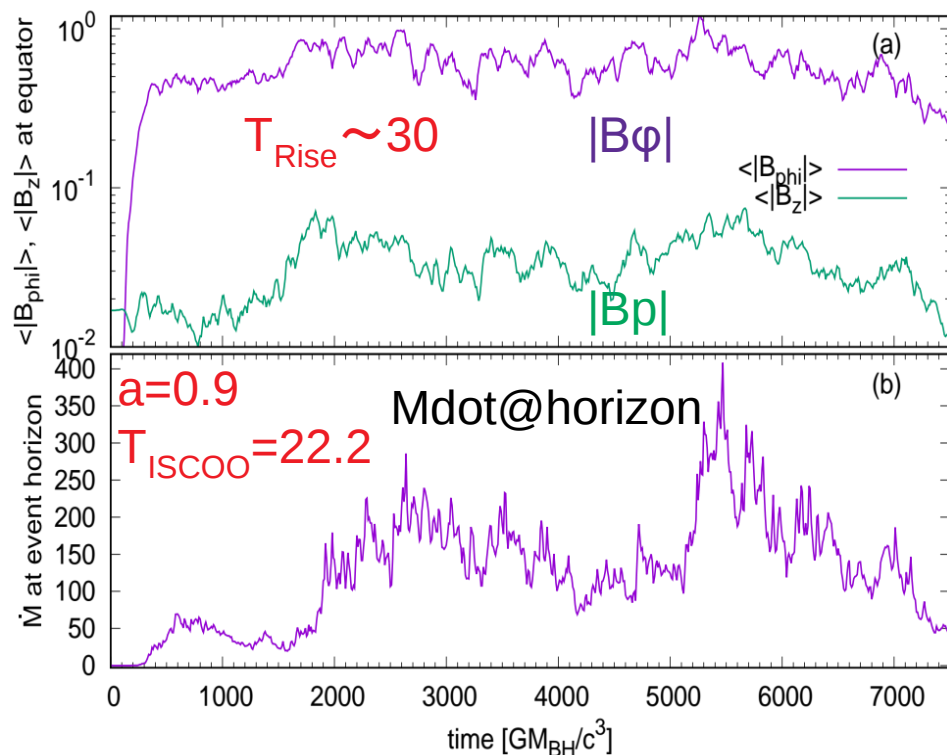
$$r_H = 1 + \sqrt{1 - a^2} \quad (g_{rr}=0 \text{ @ Boyer-Lindquist})$$

$$r_{ISCO} = 3 + g(a) \mp \sqrt{[3 - f(a)][3 + f(a) + 2g(a)]}$$

$$f(a) \equiv 1 + (1 - a^2)^{1/3}[(1 + a)^{1/3} + (1 - a)^{1/3}]$$

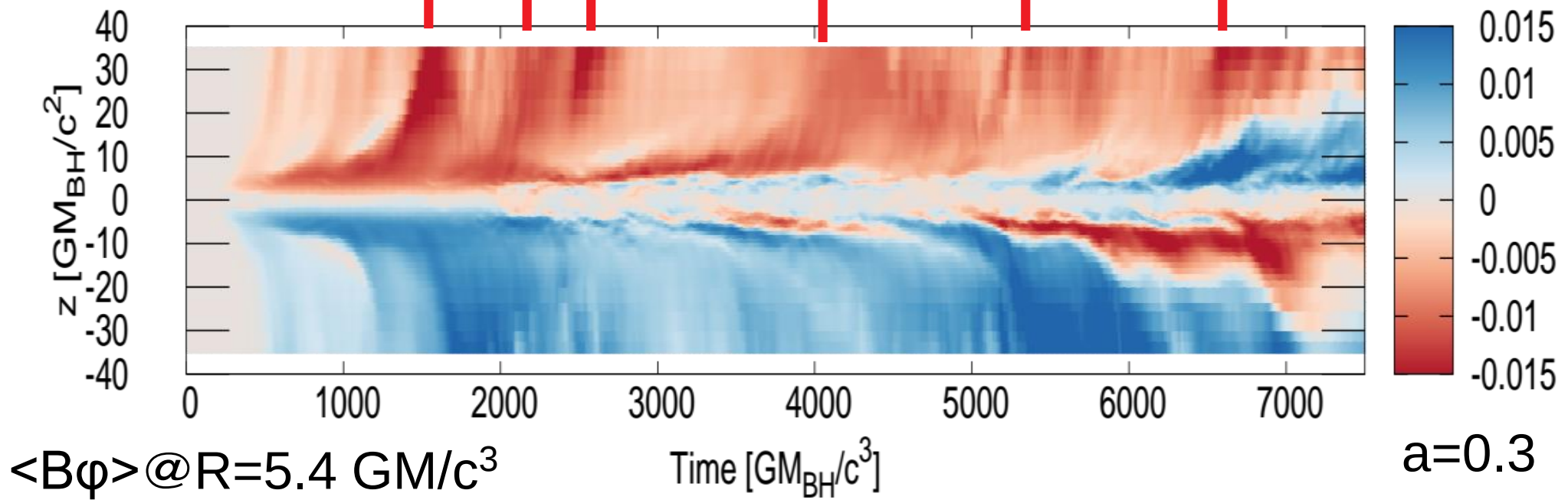
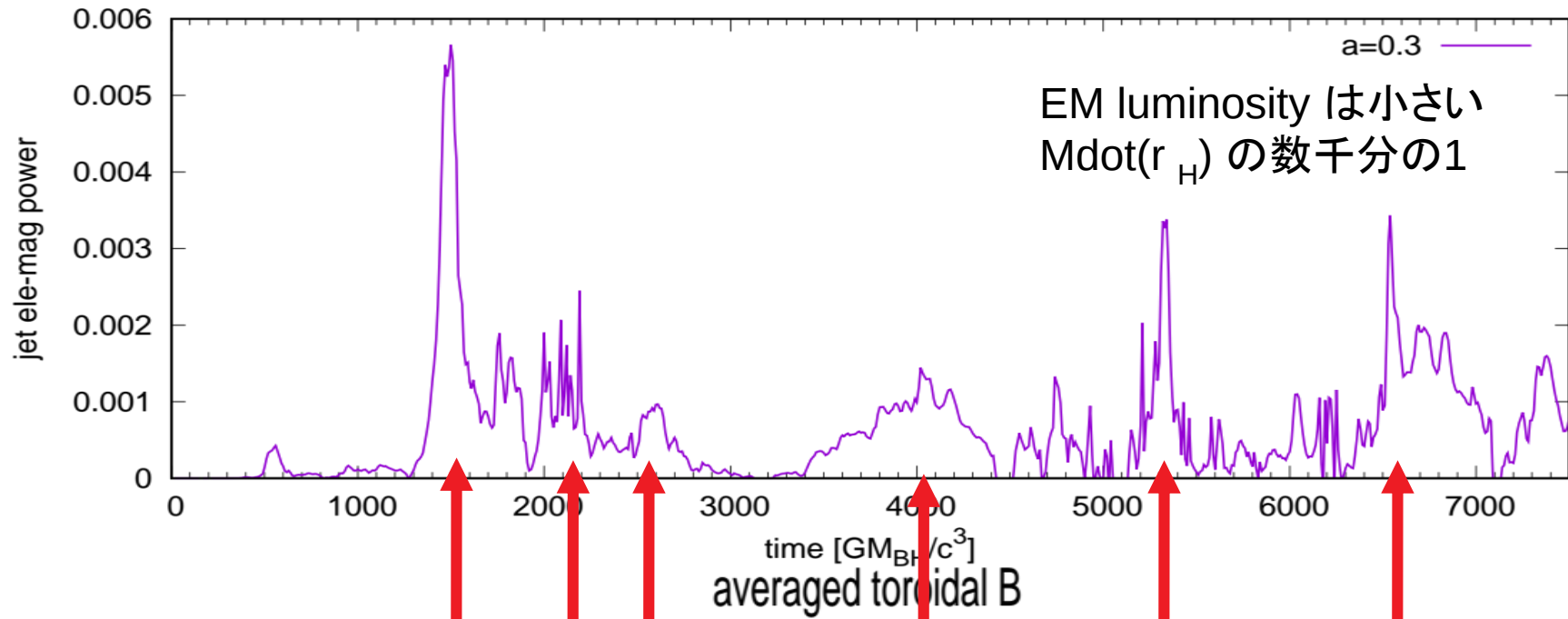
$$g(a) \equiv \sqrt{(3a^2 + f(a)^2)}$$

スピンパラメータ(a)依存性: 磁場増幅の時間スケール



- スピンパラメータ a が小さくなるにつれ、磁場増幅、質量降着率の時間変動は長くなる
- その時間スケールは ISCO 半径のやや外側でMRIによる磁場増幅の最大成長率のモードの時間スケール程度

Butterfly diagram & EM jet power



Pondermotive 力による粒子加速

- ジェット中に円盤の活動性を起源とする電磁フレア
- strength parameter a_0 at maximum peak in Alfven flare highly exceeds unity as estimated in Ebisuzaki & Tajima (2014);

$$a_0 = \frac{eE}{m_e \omega_A c} = 8.8 \times 10^{10} \left(\frac{M}{10^8 M_\odot} \right)^{1/2} \left(\frac{\dot{M}_{av} c^2}{0.1 L_{Ed}} \right)^{1/2}$$

- ジェットの密度が下がることによりAlfven wave=>EM wave
Ponderomotive 力によって荷電粒子が加速される

relativistic Alfven wave

electrons

1:1

protons

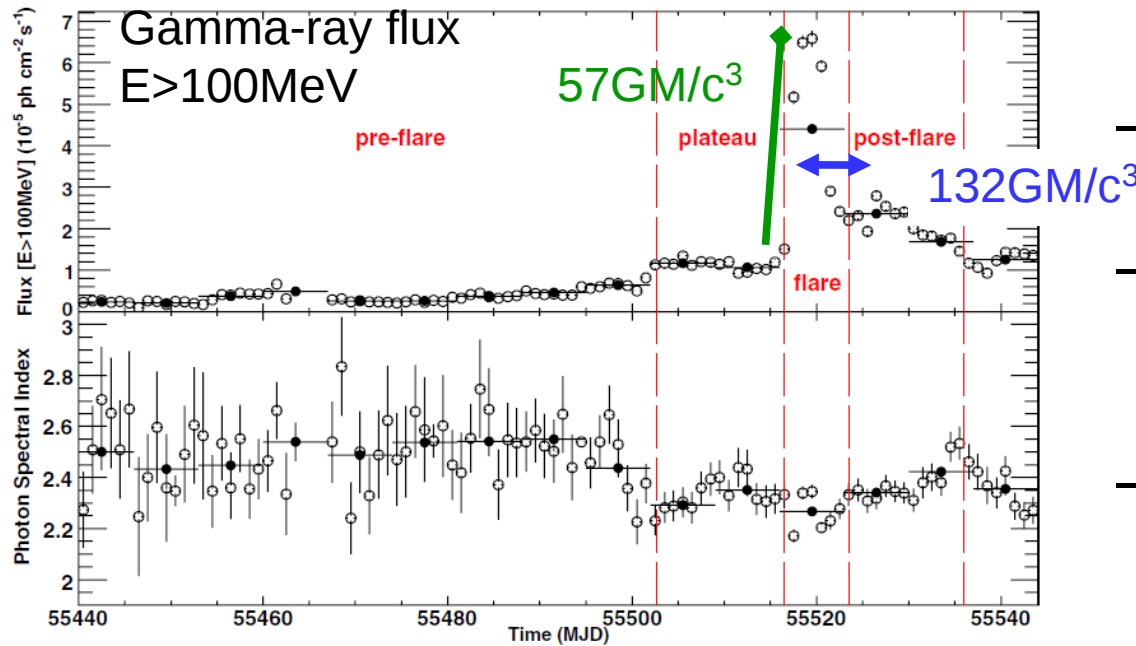
gamma-rays

– blazars

cosmic rays

Ebisuzaki & Tajima 2014

フェルガンマ線観測衛星によるガンマ線フレア



Fermi observation Abdo + ApJ 2010

- 相対論的アルフヴェン波の放射 ($a_0 \gg 1$)
- 電磁波モードへの変換
- べき的分布をする
加速された電子＋磁場
- シンクロトロン放射、
逆コンプトン放射(ガンマ線)

	our results	3C454.3	AO0235+164
rising timescale of flares ($\bar{\tau}_1$)	30	57^a	325^b
repeat cycle of flares ($\bar{\tau}_2$)	100	132^a	433^b

3C454.3 ($M_{\text{BH}} \sim 5 \times 10^8 M_{\text{sun}}$ Bonnoli et al. 2011)

まとめ

3D GRMHD simulations of rotating BH+accretion disk

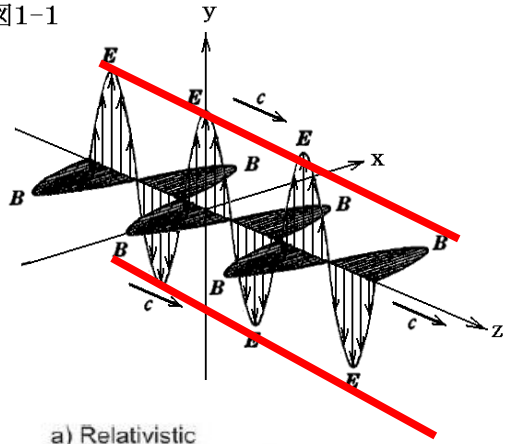
- MRI による磁場増幅と磁気散逸に伴う時間変動
 - カースピンパラメータ a が大きくなると
時間変動小、jet のPoynting 光度大
- アルフヴェンパルスの放射
 - 赤道面付近での磁場の増幅期から散逸期
 - 円盤鉛直方向
 - 一部はジェットに伝わり、ポインティング成分の
時間変動の起源に
 - 荷電粒子の加速(proton:UHECR, electron blazars)

今後 極軸付近を含めた高解像度計算

Wakefield acceleration (Tajima & Dawson PRL 1979)

Acceleration mechanism by interaction between wave and plasma.

Fig 1-1



Laser plasma
interaction
 $\Rightarrow$ 8 shape motion.

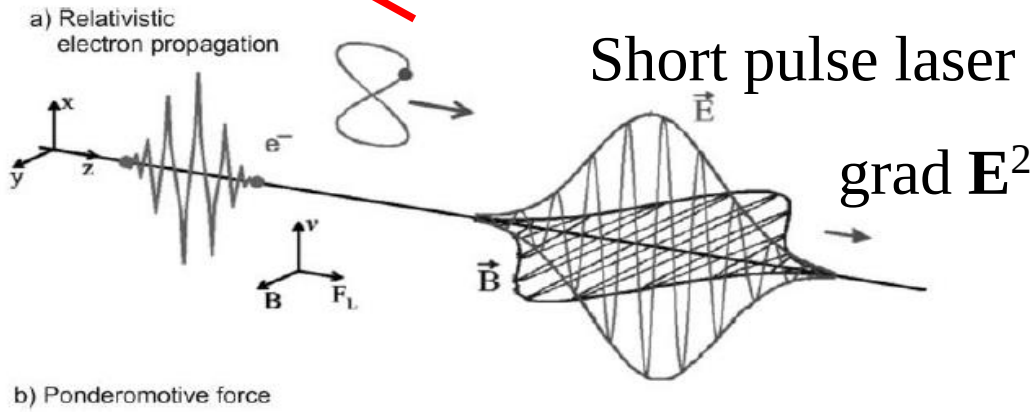
$$\mathbf{F} = q \left(\mathbf{E} + \frac{\mathbf{v}}{c} \times \mathbf{B} \right)$$

Oscillation by Electric field $\Rightarrow \mathbf{v}$
(oscillation up, down)
 $\mathbf{v} \times \mathbf{B}$ force $\Rightarrow$ oscillation forward
and backward.

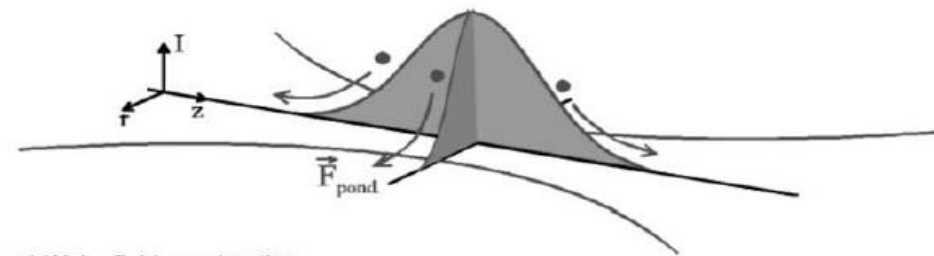
$|\mathbf{v}| \sim c \Rightarrow$ large amplification motion
by $\mathbf{v} \times \mathbf{B}$. (8 shape motion).

If there is gradient in E^2 , charged
particles feel the force towards the E^2
side. = "Ponderomotive force"

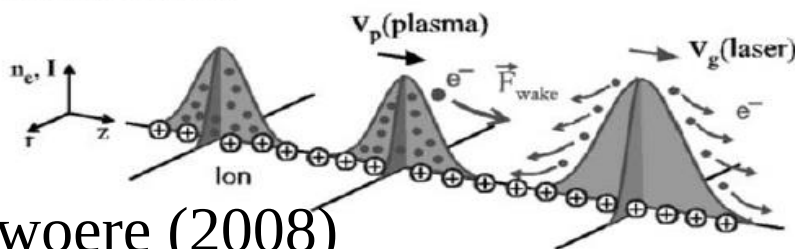
Effective acceleration for
 $I \sim 10^{18} \text{ W/cm}^2$ (relativistic intensity).
Experimentally observed.



b) Ponderomotive force



c) Wake field acceleration



Schwore (2008)

Relativistic Alfvén wave can be applied to wakefield
acceleration. (Takahashi+2000, Chen+2002,
Lyubarsky 2006, Hoshino 2008)